

A Novel Filter-Wrapper Hybrid Greedy Ensemble Approach Optimized Using the Genetic Algorithm to Reduce the Dimensionality of High-Dimensional Biomedical Datasets

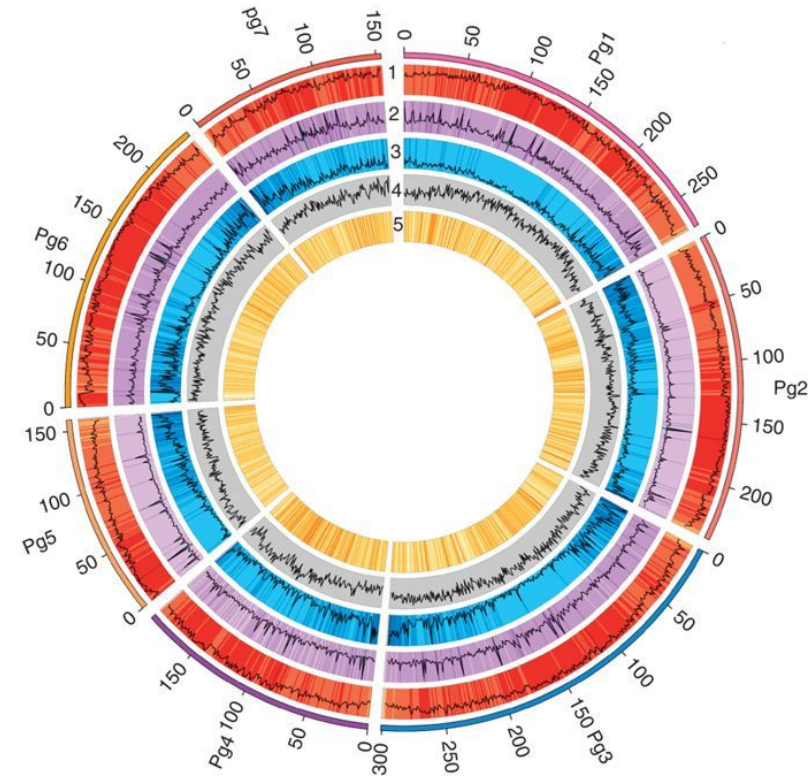
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Introduction

- ❖ Whether **more information** leads to more informed decision making?
 - ❖ **Irrelevancy**: low learnability
 - ❖ **Redundancy**: high training time
 - ❖ **Noise**: classification errors
 - ❖ **Computation cost**: expensive
- ❖ How to **choose a feature selection approach** that matches the problem structure and captures the inherent patterns in the data?
 - ❖ **Intuition-based**: unreliable
 - ❖ **Brute force**: infeasible
 - ❖ **Determine heuristically**: convergence?



Large number of features can be extracted using genome sequences*

*Varshney et al. "Pearl millet genome sequence provides a resource to improve agronomic traits in arid environments." Nature (2017).

Literature Survey

Work(s)	Methodology	Highlights	Remarks
Tu et al. 2019 [1]	Multi-strategy grey wolf optimization with three search strategies and parameter optimization	Effective feature Selection with disperse foraging	Heuristic search with convergence problem
Dong et al. 2018 [2]	Hybrid genetic algorithm with feature granulation	Faster feature selection due to bottom-up search	Heuristic search not guided by correlation
Masood et al. 2017 [3]	Hybrid and wrapper algorithms based on an incremental search using an ELM classifier	RIG and ELM based feature selection with good performance	Extremely data specific
Min et al. 2014 [4]	Backtracking and heuristic search algorithm to search for optimal feature subspaces	Similar performance of backtracking and heuristic algorithms	Heuristic search with convergence problem
Ekwevugbe et al. 2013 [5]	Filter approaches to determine the optimal feature subspace	Correlation-based approaches with faster training	Classifier independence limits accuracy

Outcome of Literature Survey

- ❖ **Which feature selection?:** multiple filter, wrapper, embedded, hybrid, and heuristic approaches; which one accurately matches the problem structure? always an issue
- ❖ **Filter-based approaches:** faster computation, but heavily dependence on correlation and classifier independence limits their accuracy
- ❖ **Wrapper-based, embedded, and hybrid approaches:** domain adaptability and high computational cost of training, but reliable performance
- ❖ **Metaheuristic search approaches:** population-based mechanism guides the search, but convergence problem and correlation-unguided search can be a bottleneck!
- ❖ **Need for an ensemble?:** set of predetermined feature selection approaches
 - ❖ **Voting-based ensemble?:** simply a brute force ensemble inefficient
 - ❖ **Greedy ensemble?:** penalize bad-performing selection methods and their features
- ❖ **Time and accuracy tradeoff:** use a hybrid of filter and wrapper approaches

Key Contributions

Aim: Generate an optimal and instructive feature subspace with a lower computational complexity

- ❖ Design of a **filter-wrapper hybrid ensemble selection approach** that kindles an optimal feature subspace by **greedily** combining the subspaces generated by various predetermined feature selection techniques based on specific performance dependant penalty parameters
- ❖ Leveraging **heuristic search strategies** such as greedy parameter-wise optimization and GA to determine the optimal values of the **penalty factors** which affect how different feature subspaces are ensembled to engender an optimal feature subspace
- ❖ We present detailed **benchmarking results** of our hybrid greedy ensemble feature selection approach on three distinct high-dimensional biomedical datasets. Our experimental results indicate the **efficiency** and **robustness** of the proposed approach over the base feature selection methods, and other prolific filter and wrapper methods

Biomedical Datasets

Dataset	#Samples	#Dimensions	#Classes (#samples per class)	Balanced?
TIS ^[6]	13,375	927	2 (3,312; 10,063)	No
Skin Cancer ^[7]	10,015	2,352	7 (327; 514; 1,099; 115; 6,705; 142; 1,113)	No
Seizure ^[8]	11,500	179	5 (2,300; 2,300; 2,300; 2,300; 2,300)	Yes

- ❖ **TIS**: extracted from genomic sequences of a selected set of vertebrates (from GenBank), involving the process of finding sites where translation of mRNA to proteins initiates
- ❖ **Skin Cancer**: extracted from the pixel information of 28×28 RGB dermatoscopic images of the Skin Cancer MNIST: HAM10000 dataset
- ❖ **Epileptic Seizure Recognition**: consists of five sets of single channel 23.6 seconds long electroencephalogram segments that are weakly stationary and selected after a visual inspection of artifacts

Proposed Methodology

Feature selection using the selected methods

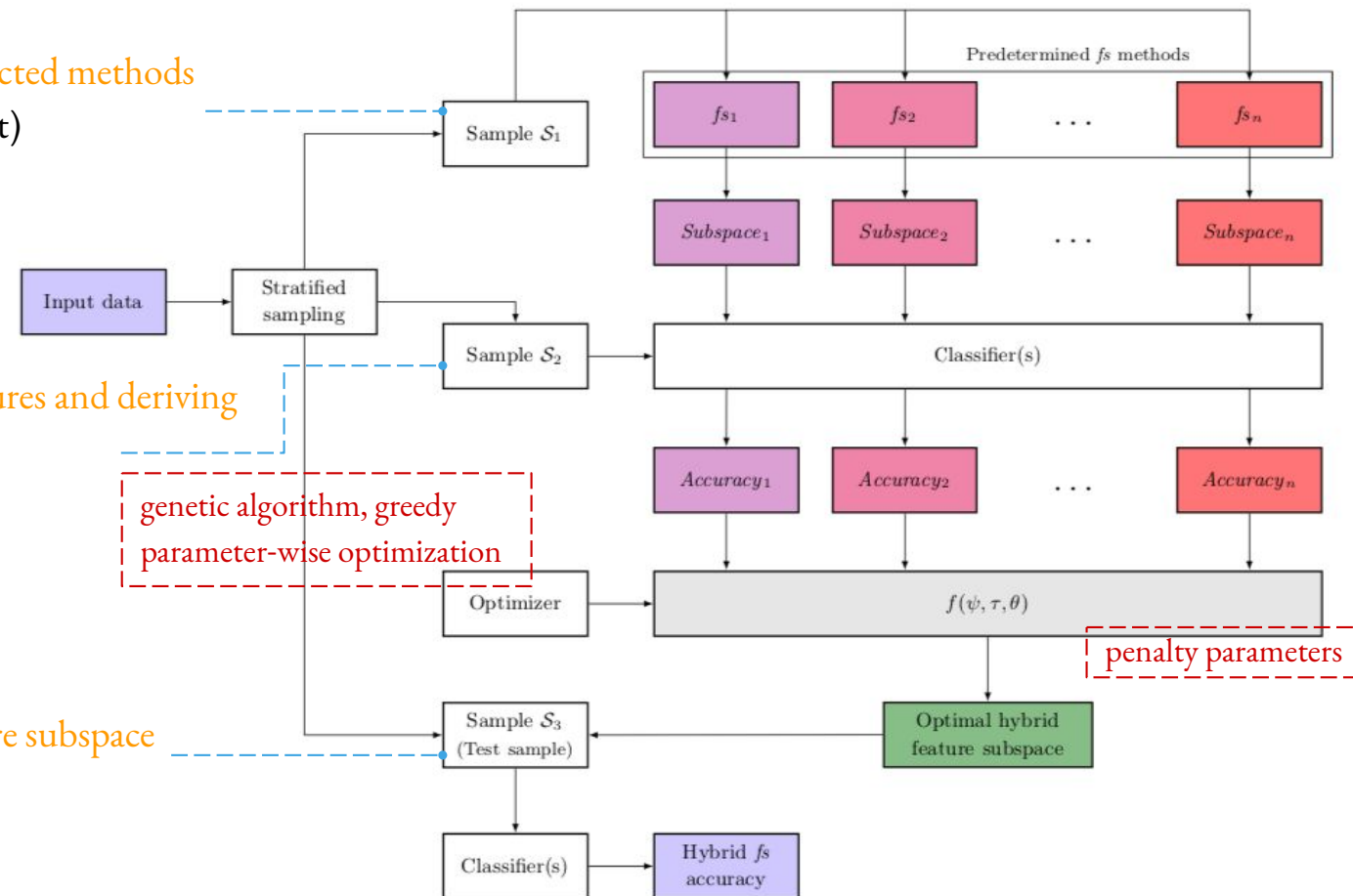
Feature space: #features(dataset)

Evaluation of the selected features and deriving the hybrid feature subspace

Feature space: #features(S_1)

Evaluation of the hybrid feature subspace

Feature space: hybrid



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Filter-Wrapper Hybrid Greedy Ensemble

Algorithm 1: Proposed hybrid greedy ensemble feature selection

Input: S_2 -All-Features-Acc: Average accuracy with all features of S_2 ,
 S_2 -Accuracies: List of average accuracies from predetermined methods,
 \mathcal{FS} -Lists: List of all selected feature subsets,
totalFeat: Total number of features in the given dataset,
 ρ_m -List: List of ranks of predetermined selection methods,
 ψ : Accuracy penalty parameter,
 τ : Feature penalty parameter,
 θ : Selection threshold.

Output: Hybrid \mathcal{FS} : Greedily selected optimal feature subset.

```

1: accScores  $\leftarrow$  [0] *  $|\mathcal{FS}\text{-Lists}|$ 
2: overallScores  $\leftarrow$  [0] * totalFeat
3: for  $idx \leftarrow 0$  to  $|\mathcal{FS}\text{-Lists}|$  do
4:   accScores[idx]  $\leftarrow$  accScore(method,  $|\mathcal{FS}\text{-Lists}|$ ,  $\rho_m\text{-List}[idx]$ )
5:   if  $S_2\text{-Accuracies}[idx] < S_2\text{-All-Features-Acc}$  then
6:     accScores[idx]  $\leftarrow$  accScores[idx]/ $\psi$ 
7:   end
8:   for  $featIdx \leftarrow 0$  to totalFeat do
9:     featScore  $\leftarrow$  featScore(feats,  $\mathcal{FS}\text{-Lists}[idx]$ , featIdx + 1)
10:    if  $S_2\text{-Accuracies}[idx] > S_2\text{-All-Features-Acc}$  and  $feat \notin \mathcal{FS}\text{-Lists}[idx]$  then
11:      featScore  $\leftarrow$  featScore *  $\tau$ 
12:    end
13:    overallScore  $\leftarrow$  featScore * accScores[idx]
14:    overallScores[featIdx]  $\leftarrow$  overallScores[featIdx] + overallScore
15:  end
16: end
17: hybridFeatures  $\leftarrow$  []
18: for  $score \in$  overallScores do
19:   if  $score > \theta$  then
20:     hybridFeatures.append(feats)
21:   end
22: end
23: return hybridFeatures

```

❖ Scoring of features (**featScore**) and selection methods (**accScore**):

$$featScore(f, \mathcal{FS}, \rho_f) = \begin{cases} \frac{|\mathcal{FS}| - \rho_f + 1}{|\mathcal{FS}|}, & f \in \text{ranked } \mathcal{FS} \\ \frac{1}{|\mathcal{FS}|}, & f \in \text{unranked } \mathcal{FS} \\ \frac{-1}{|\mathcal{FS}|}, & f \notin \mathcal{FS} \end{cases}$$

$$accScore(m, \mathcal{M}, \rho_m) = \frac{|\mathcal{M}| - \rho_m + 1}{|\mathcal{M}|}$$

❖ **Penalty parameters** for greedy ensembling of base feature subspaces

❖ **Accuracy penalty:** $accScore/\psi$

❖ **Feature penalty:** $featScore \times \tau$

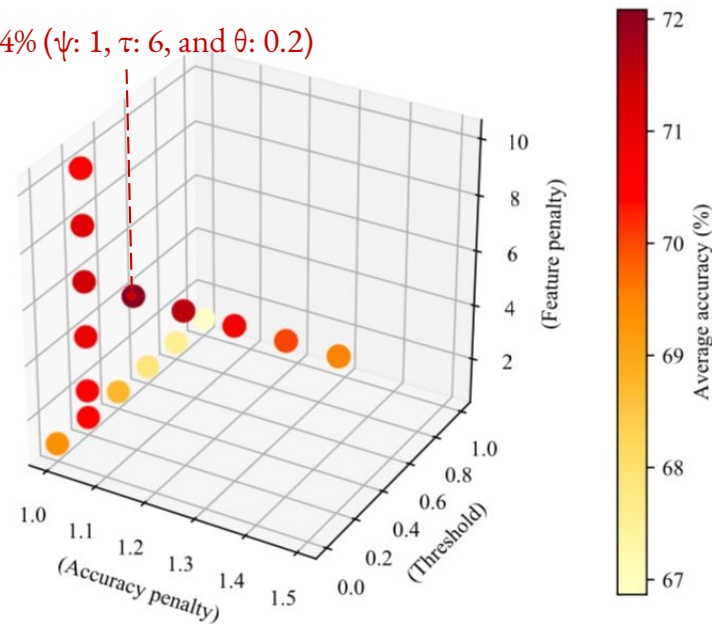
❖ **Overall feature scoring** and hybrid feature selection (θ):

$$overallScore(f, \mathcal{M}) = \sum_m^{\mathcal{M}} featScore(f) \times accScore(m)$$

❖ **Optimization** of penalty parameters

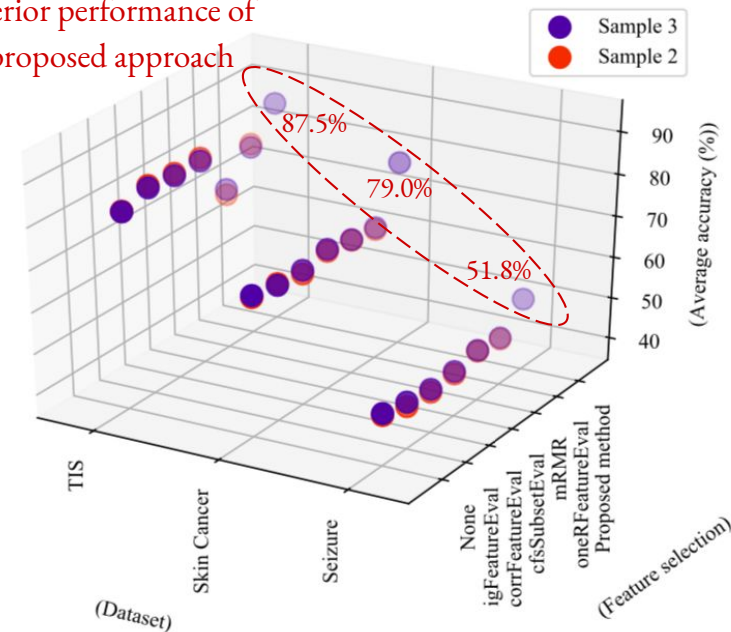
Results with Optimization of Penalty Parameters

71.354% ($\psi: 1, \tau: 6, \text{ and } \theta: 0.2$)



The effect of $\psi, \tau, \text{ and } \theta$ on Skin Cancer dataset (greedy parameter-wise optimization)

Superior performance of the proposed approach



The effect of $\psi, \tau, \text{ and } \theta$ on Skin Cancer dataset (genetic algorithm ($N = 50, p_c = 0.6, p_m = 0.1$))

Results with Genetic Optimization: Comparison

Dataset	Chromosome			Sample (S_3) Average Accuracy (%)	
	ψ	τ	θ	Base Selection Method (Highest)	Proposed Ensemble
TIS ^[6]	6.08	20.83	0.78	IgFeatureEval: 83.948	87.449
Skin Cancer ^[7]	1.07	7.72	0.14	CfsSubsetEval: 68.534	78.912
Seizure ^[8]	1.39	2.58	0.01	None: 47.131	51.811

Dataset	Sample (S_3) Average Accuracy (%)				Proposed Greedy Ensemble
	Filter Approaches		Wrapper Approaches		
	RF Feature Importance	Chi-Square Test	RFE + SVM (Linear)	RFE + SVM (RBF)	
TIS ^[6]	84.182	84.220	79.968	83.290	87.449
Skin Cancer ^[7]	67.356	67.794	67.307	67.375	78.912
Seizure ^[8]	46.601	46.299	46.818	50.450	51.811

Conclusions and Future Work

- ❖ Proposed a penalty based **filter-wrapper hybrid greedy ensemble** approach to facilitate optimal feature selection
- ❖ Ensemble **greedily** selects the features from the subspaces obtained from the predetermined base selection methods
- ❖ Specific **performance dependent penalty parameters** were used to penalize the base feature subspaces essential to achieve the optimal ensembling of those subspaces
- ❖ At any point in time, only a stratified sample and not the entire dataset is not used for computation; the computational complexity is significantly reduced
- ❖ We leverage **effective heuristic search strategies** including the greedy parameter-wise optimization and the GA to obtain optimal values of the penalty parameters
- ❖ The proposed method introduces additional (penalty) parameters which **require prior training** to obtain the optimal setting in advance

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