

A novel filter-wrapper hybrid greedy ensemble approach optimized using the genetic algorithm to reduce the dimensionality of high-dimensional biomedical datasets[☆]

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Abstract

The predictive accuracy of high-dimensional biomedical datasets is often dwindled by many irrelevant and redundant molecular disease diagnosis features. Dimensionality reduction aims at finding a feature subspace that preserves the predictive accuracy while eliminating noise and curtailing the high computational cost of training. The applicability of a particular feature selection technique is heavily reliant on the ability of that technique to match the problem structure and to capture the inherent patterns in the data. In this paper, we propose a novel filter-wrapper hybrid ensemble feature selection approach based on the weighted occurrence frequency and the penalty scheme, to obtain the most discriminative and instructive feature subspace. The proposed approach engenders an optimal feature subspace by greedily combining the feature subspaces obtained from various predetermined base feature selection techniques. Furthermore, the base feature subspaces are penalized based on specific performance dependent penalty parameters. We leverage effective heuristic search strategies including the greedy parameter-wise optimization and the Genetic Algorithm (GA) to optimize the subspace ensembling process. The effectiveness, robustness, and flexibility of the proposed hybrid greedy ensemble approach in comparison with the base feature selection techniques, and prolific filter and state-of-the-art wrapper methods are justified by empirical analysis on three distinct high-dimensional biomedical datasets. Experimental validation revealed that the proposed greedy approach, when optimized using GA, outperformed the selected base feature selection techniques by 4.17%–15.14% in terms of the

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prediction accuracy.

Keywords: Biomedical data, Genetic algorithm, Greedy ensemble, High-dimensional data, Hybrid feature selection, Parameter optimization.

1. Introduction

The need for efficient analytical methodologies in healthcare applications has led to an unparalleled development in the field of biomedicine and bioinformatics over the past decade [41, 62]. Research in these fields frequently encounters supervised classification of disease data (e.g., microarray gene data, lung cancer data, and others) [41, 14, 2]. The advances in wet-technology are increasing the volume of data with a large number of dimensions [33]. For example, the profiling of microarray gene [33, 10, 34] aims at measuring the expression levels of tens of thousands of genes over tens of thousands of features. Over the last decade, owing to the availability of high dimensional biomedical data, numerous feature selection methods have become viable processes that provide robust data in low-dimensional spaces [55, 25]. In the sense of high dimensional data, standard statistical methods suffer from the curse of dimensionality [8, 30] signifying a drastic rise in the classification error and computational complexity. This makes it mandatory to use a feature subspace before the classification is undertaken [50, 54, 28]. Therefore, feature selection does not represent the very aim of data analysis but is instead a preliminary step to finding the most informative and discriminative feature subset that optimally represents the given data.

Dimensionality reduction can aid in the provision of better insights to understanding causal relationships, reduce computational complexities, and engender more reliable estimates [61, 12]. There are numerous methods to achieve dimensionality reduction including feature selection based on information gain and minimum Redundancy Maximum Relevance (mRMR). Real-world datasets vary, implying that no single feature selection technique is best suited for all the datasets [18]. The effectiveness of a feature selection technique depends on its ability to match the problem structure and maintain only those features that describe the inherent patterns within the data. The selection of such a technique is usually heuristic and intuition based. The challenge to the machine learner is the selection of a feature selection technique that works best for a given dataset. A naive approach to achieve the same would be to select a technique from the set of predetermined techniques that results in the best performance. This approach is computationally very expensive and infeasible. An alternative approach would be to perform a heuristic selection which is further explored using evolutionary computational algorithms [29]. This approach requires an investment of an arbitrary amount of computation time, and the actual optimal solution and the obtained solution might not converge for a limited number of iterations [1, 22].

Early works [15, 17, 69] aimed at using filter approaches to determine the most optimal feature subspace. These approaches are heavily reliant on the

Table 1: Comparison with state-of-the-art works in feature selection.

	Masood <i>et al.</i> 2017	Dong <i>et al.</i> 2018	Tu <i>et al.</i> 2019	This work
Feature selection type	Wrapper and filter-wrapper hybrid	Heuristic search	Heuristic search	Filter-wrapper hybrid with heuristic search
Approaches used	Wrapper and hybrid approaches	Hybrid GA with granularity	Multi-strategy ensemble grey wolf optimizer	Hybrid greedy ensemble selection approach
Ensembling	–	–	3 search strategies	5 filter-wrapper hybrid methods
Search strategy	–	Bottom-up search of ordered feature list	Grey wolf optimizer	Correlation-guided greedy feature search
Parameter optimization	–	GA	Disperse foraging strategy	Greedy-parameter wise optimization and GA
Max. #features	21 ($\times 4$ sensors)	12,582	60	2,352
Corresponding #samples	28 (occupants)	72	208	10,015
Corresponding #classes	4	10	3	7
Algorithms used	RIG ^a and ELM	–	–	RF ^b , BDT ^c , and KNN ^d

^aRelative Information Gain; ^bRandom Forest; ^cBagged Decision Tree; ^dK-Nearest Neighbors.

41 correlation between the features and are independent of the classifier which
42 limits their accuracy. Min *et al.* [45] developed a backtracking and heuristic
43 search algorithm to search for optimal feature subspaces. The authors showed
44 that the performance of the evolutionary computing algorithm was similar to
45 backtracking but with lower computational time. More recently, Masood *et al.*
46 [42] proposed wrapper and hybrid algorithms which used an incremental
47 search on an ordered set of features and Extreme Learning Machine (ELM)
48 classifier to select the best feature subspace. A hybrid genetic algorithm with
49 feature granulation was developed by Dong *et al.* [16] for feature selection.
50 Tu *et al.* [64] proposed a multi-strategy ensemble grey wolf optimizer with
51 three search strategies and demonstrated its effectiveness in selecting optimal
52 features. From the existing literature, it is evident that hybrid and wrapper
53 feature selection methods overcome the limitations of filter methods. Moreover,
54 evolutionary computing algorithms are widely used in feature selection because
55 of their population-based mechanism and domain adaptability.

56 Although most state-of-the-art methods aim at effectively determining an
57 optimal feature subspace, they are either extremely data specific or utilize
58 heuristic-based approaches requiring an arbitrary amount of time with no guar-
59 antee on their convergence. Furthermore, heuristic search methods using swarm
60 intelligence seldom use correlation measures to guide the search process. To ad-
61 dress these problems, we propose a novel ensemble selection approach that uses
62 a set of (five) predetermined feature selection techniques on a representative

63 sample of the dataset to generate multiple feature subspaces. These subspaces
64 are then evaluated using (three) different supervised classification algorithms.
65 The features in the subspaces obtained from the set of chosen feature selection
66 techniques are then penalized based on the evaluation scores, to form an optimal
67 subset of features selected greedily. The penalty factors that affect the choice
68 of features in the hybrid subset are optimized using the greedy parameter-wise
69 optimization and the Genetic Algorithm (GA). Moreover, the penalty factors
70 are modeled in a way that is aimed at selecting smaller and most instructive
71 feature subspace. Since the feature selection is performed on a sample of the
72 dataset as opposed to the entire dataset, the computational cost is relatively
73 low. Furthermore, the values of the penalty factors that affect the choice of the
74 features in the final feature subspace are heuristically determined, limiting the
75 problem of algorithmic convergence occurring when the features themselves are
76 heuristically selected. Table 1 shows the comparison of this work with the exist-
77 ing state-of-the-art methods in effective feature selection. The key contributions
78 of this work are summarized below:

- 79 • Design of a filter-wrapper hybrid ensemble selection approach that kin-
80 dles an optimal feature subspace by greedily combining the subspaces
81 generated by various predetermined feature selection techniques based on
82 specific performance dependent penalty parameters.

- 83 • Leveraging heuristic search strategies such as greedy parameter-wise op-
84 timization and GA to determine the optimal values of the penalty factors
85 which affect how different feature subspaces are ensembled to engender an
86 optimal feature subspace.

- 87 • We present detailed benchmarking results of our hybrid greedy ensemble
88 feature selection approach on three distinct high-dimensional biomedical
89 datasets. Our experimental results indicate the efficiency and robustness
90 of the proposed approach over the base feature selection methods, and
91 other prolific filter and wrapper methods.

92 The remainder of the paper is structured as follows: Section 2 provides an
93 overview of the existing works and reviews their evaluation approaches, advan-
94 tages, and limitations. Section 3 presents the statistics of the datasets used and
95 addresses the fundamentals of the utilized feature selection algorithms, classifi-
96 cation algorithms, and GA. The proposed greedy methodology is presented in
97 Section 4 and the same is evaluated empirically in Section 5. In Section 6, a
98 sensitivity analysis is presented to assess the performance of the results. Finally,
99 Section 7 concludes this paper with highlights on future research possibilities.

100 2. Related work

101 An extensive body of research on the effective determination of most descrip-
102 tive feature subspace is available in the literature [60, 3]. This section provides
103 an extensive review of a few significant dimensionality reduction approaches

104 to provide an overview of the existing state-of-the-art methods built on large
105 biomedical datasets.

106 Feature selection approaches can be categorized into four categories includ-
107 ing filter, wrapper, embedded, and hybrid models. In the field of biomedicine,
108 feature selection is widely used in sequence analysis (signal analysis and content
109 analysis) [31] and microarray analysis. Sequence analysis aims at the deter-
110 mination of the sequence (e.g., carbohydrates, proteins, and others), its frag-
111 mentation, and its interpretation. Apart from the features that represent amino
112 acid or nucleotide, many other features resulting from the combinations of these
113 building blocks can be derived. Since most of these features are redundant or
114 irrelevant, feature selection techniques are mandatory to derive a subset of rele-
115 vant features [55]. Moreover, most features are extracted from a sequence where
116 adjacent positions in the sequence hold most dependencies. Early works [56, 4]
117 developed and used interpolated Markov model which used the interpolation
118 between various Markov model's orders to deal with the limited number of sam-
119 ples of small sizes. The model was further extended to deal with non-adjacent
120 dependencies by using feature subset sampling with undersampling of majority
121 class. These previous works showed significant performance improvement using
122 Support Vector Machines (SVM) with full undersampling and feature selection.

123 A more trending area of research is the microarray analysis, where structural
124 elements such as splice sites, Translation Initiation Sites (TIS) are modeled as
125 classification problems [55]. Microarray analysis uses gene expression profiling
126 of tissues or cell samples to determine which combination of genes are turned
127 on. Microarray datasets pose challenges to modeling due to their low samples-
128 to-dimensions ratio [2]. Li and Yen [35] proposed an optimization based on
129 multiobjective binary biogeography (filter approach), with SVM classifier, and
130 evaluated the computational complexity of their approach on multiple datasets.
131 Liao *et al.* [37] used a filter method of selecting genes based on locality-sensitive
132 Laplacian scoring scheme, with SVM classifier. The authors evaluated their ap-
133 proach using a variety of datasets including Leukemia and Lung Cancer datasets.
134 From the criterion of accuracy, it can be inferred that the early works which
135 used filter-based feature selection techniques suffered from the limitation that
136 the correlation measure used to assess the importance of features is classifier
137 independent.

138 Wrapper, hybrid, and embedded approaches address the limitations of filter-
139 based approaches. Sharma *et al.* [58] proposed a wrapper-based approach to
140 select features based on null space linear discriminant analysis, with K-Nearest
141 Neighbors (KNN), evaluated the approach using sensitivity analysis. Yu *et al.*
142 [67] used sample weighting to select stable genes from microarray data using
143 recursive feature elimination with SVM (wrapper approach). Liu *et al.* [38]
144 proposed a hybrid feature selection approach that involved the usage of Bhat-
145 tacharyya distance as the filter and fuzzy interactive self-organizing algorithm
146 as the wrapper. Hajiloo *et al.* [23] proposed a hybrid method of rule-based
147 classification using fuzzy SVM as the wrapper and signal-to-noise ratio as the
148 filter. Masood *et al.* [42] presented wrapper and hybrid algorithms which used
149 bottom-up incremental search on an ordered set of features. The authors used

Table 2: Summary of some key existing works.

Work	Feature selection approach	Classifier	Evaluation method
Liu <i>et al.</i> [39]	Wrapper approach based on the fuzzy interactive self-organizing data algorithm for sample selection	KNN, Linear SVM	Recognition rate, Area Under Curve (AUC)
Chang <i>et al.</i> [13]	Hybrid feature selection method using GA, ReliefF and adaptive neuro-fuzzy inference system	Neural net, SVM, Logistic regression, Fuzzy system	AUC, K-fold cross-validation
Liang <i>et al.</i> [36]	An embedded method with regularized multinomial sparse logistic regression with $L_{1/2}$ penalty	KNN	Leave one-out cross-validation
Song <i>et al.</i> [59]	Fast ensemble method that selects feature subsets using graph-theoretic clustering techniques	Naive Bayes, C4.5, IB1, Rule-based RIPPER ^e	Sensitivity, K-fold cross-validation, Runtime
Maulik and Chakraborty [43]	Filter approach that uses rough set based on prediction scheme using fuzzy preference for Cancer datasets	Transductive SVM	K-fold cross-validation
Yu <i>et al.</i> [68]	An ensemble semi-supervised clustering approach based on modified double selection for tumor clustering	K-means clustering	SD ^f and Mean of normalized MI ^g

^e Repeated Incremental Pruning to Produce Error Reduction;
^f Standard Deviation; ^g Mutual Information.

150 ELM for the incremental search and relative information gain for feature rank-
151 ing. Gaafar *et al.* [19] proposed an ensemble selection method based on mRMR
152 and GA, with KNN classifier for cancer diagnosis using microarray data. Table
153 2 reviews other related key existing works in the field of feature selection in
154 biomedicine and bioinformatics. Although wrapper, hybrid, and embedded ap-
155 proaches overcome the limitations of filter-based approaches by ensuring lower
156 error of the model, they are highly dataset and classifier specific. The challenge
157 of the selection of a dimensionality reduction technique that effectively matches
158 the problem structure is quite difficult and is often heuristic or intuition based.

159 More recently, metaheuristic search optimizations such as GA and parti-
160 cle swarm optimization have been applied to search for the optimal feature
161 subspace. In comparison with the traditional methods, metaheuristic search
162 approaches do not make assumptions about the search space (e.g., differen-
163 tiable and linearly separable). Furthermore, the success of these swarm intel-
164 ligence algorithms can be attributed to their versatility and flexibility, in the

165 sense that they mimic the best features in nature. Dong *et al.* [16] proposed
166 a hybrid genetic algorithm with feature granulation to select significant fea-
167 tures. To improve the quality of the feature subset, the authors developed an
168 improved neighborhood rough set approach with sample granulation. Tu *et al.*
169 [64] proposed a multi-strategy ensemble grey wolf optimizer to select the feature
170 subspace effectively. Furthermore, the authors used a parameter self-adjusting
171 strategy to balance between exploitation and exploration of the feature space.
172 Even though evolutionary computing algorithms overcome the limitations of the
173 wrapper and hybrid methods, they are reliant on heuristic search requiring an
174 arbitrary amount of time with no guarantee on the convergence of the obtained
175 solution within the given number of iterations. Furthermore, these swarm intel-
176 ligence algorithms seldom use correlation measure to guide the search process.

177 Our work advances the efforts of these previous state-of-the-art methods
178 by using a novel filter-wrapper hybrid ensemble feature selection approach that
179 engenders an optimal feature subspace by greedily combining the subspaces gen-
180 erated from various predetermined feature selection techniques. Furthermore,
181 the feature subspaces are penalized based on their evaluation scores with re-
182 spect to the predetermined classifier(s). Since the feature selection is performed
183 on a sample of the dataset as opposed to the entire dataset, the computational
184 cost is relatively low. Moreover, the values of the penalty parameters are de-
185 termined heuristically, limiting the convergence problem occurring when the
186 features themselves are heuristically determined.

187 3. Materials and methods

188 The experimental data consists of three biomedical datasets which are first
189 described. All the datasets used are split into three mutually and collectively
190 independent homogeneous samples using stratified random sampling [49]. Strat-
191 ified random sampling guarantees the adequate representation of all the classes
192 in the data, maintaining homogeneity within stratum and heterogeneity between
193 strata¹. The feature selection methods used in greedily deriving the hybrid fea-
194 tures are discussed, followed by the discussion of the classification algorithms
195 used in the evaluation of the feature selection techniques. Finally, the genetic
196 algorithm used in the optimization of the penalty parameters that are used in
197 deriving the hybrid feature subspace is detailed.

198 3.1. Biomedical datasets

199 The main characteristics of the datasets used in this paper are tabulated in
200 Table 3. The datasets chosen have a sufficient number of samples to aid in the
201 creation of three stratified samples. Both balanced and imbalanced datasets are
202 chosen for an unbiased evaluation of the proposed technique. Depending on the
203 size of the dataset, further sampling of the strata can be performed.

¹Proportionate allocation variant of the stratified random sampling is used in this paper.

Table 3: Overview of the datasets used.

Dataset	Size	#Dim	#Classes (#samples per class)
TIS [51]	13,375	927	2 (3,312/10,063)
Skin Cancer [63]	10,015	2,352	7 (327/514/1,099/115/6,705/142/1,113)
Seizure [5]	11,500	179	5 (2,300/2,300/2,300/2,300/2,300)

204 Translation Initiation Sites (TIS) dataset [51] is extracted from the genome
205 sequences of a selected set of vertebrates that were extracted from the GenBank
206 [9]. The process involves finding the site at which the translation of mRNA to
207 proteins initiates. The sequences are annotated with TIS (true or false). Since
208 the dataset is comprised of processed DNA sequences, the TIS site is essentially
209 an ‘ATG²’ sequence. The sequences are extracted to build a feature space by
210 matching three nucleotides to one amino acid, counting the frequency of every
211 amino acid and frequency of a pair of amino acids [32].

212 Skin Cancer dataset is extracted from the pixel information of 28×28 RGB
213 images of the Skin Cancer MNIST: HAM10000 (Human Against Machine with
214 10,000 training images) dataset [63]. The dataset comprises of a large collection
215 of dermatoscopic images of the pigmented skin lesions. The dataset consists of
216 all the important diagnostic categories of pigmented lesions including basal cell
217 carcinoma, actinic keratosis and Bowen’s disease, benign keratosis-like lesions,
218 melanoma, dermatofibroma, vascular lesions, and melanocytic nevi.

219 Epileptic Seizure Recognition dataset [5] consists of five sets ($A-E$), each
220 containing 100 single channel 23.6 seconds long electroencephalogram (EEG)
221 segments. Each EEG segment is weakly stationary and is selected after a visual
222 inspection for artifacts [20]. Surface EEG recordings of five healthy individuals
223 form sets A (with eyes closed) and B (with eyes open). Segments measured from
224 five patients in seizure-free intervals from opposite hemisphere’s hippocampal
225 formation and in the epileptogenic zone form sets C and D respectively. Seizure
226 activity corresponding to all the recording sites showing the ictal activity forms
227 set E .

228 3.2. Feature selection methods

229 The feature selection methods used to generate feature subspaces which are
230 in turn used in the generation of the hybrid feature subspace are discussed in
231 this section. Five feature selection techniques are used in this paper (four with
232 feature ranking, one without feature ranking). The implementations available in
233 Weka 3.8.3 [27] were used to implement all the predetermined feature selection
234 methods.

²Adenine(A), Thymine (T), and Guanine (G).

235 *3.2.1. Information gain-based feature selection*

236 Information gain-based feature selection (*igFeatureEval*) [6] evaluates the
 237 goodness (worth) of a feature by computing the Information Gain (IG) of a
 238 feature with respect to the target class. Concisely, IG measures the amount of
 239 information (in bits/Shannons) obtained to predict the target class by knowing
 240 the presence or absence of a feature. IG between a feature (f) and the target
 241 class is given by Equation 1, where $H(\cdot)$ represents the marginal entropy, and
 242 $H(\text{class}|f)$ measures the conditional entropy of f after observing the target class.

$$\text{IG}(f, \text{class}) = H(\text{class}) - H(\text{class}|f) \quad (1)$$

243 The *igFeatureEval* is a fast filter-based feature selection method. The se-
 244 lected features (based on the threshold) are ranked in the order of decreasing
 245 IG scores.

246 *3.2.2. Correlation-based feature selection*

247 Correlation-based feature selection (*corrFeatureEval*) [24] evaluates the good-
 248 ness (worth) of a feature by computing the Pearson’s (bi-variate) correlation
 249 (PCC) between the feature and the target class. Equation 2 gives the Pearson’s
 250 correlation measure between a feature (f) and the target class, where $E[\cdot]$ rep-
 251 represents the expected value, μ_x represents the mean of x , and σ_x represents the
 252 standard deviation of x .

$$\text{PCC}(f, \text{class}) = \frac{E[(f - \mu_f)(\text{class} - \mu_{\text{class}})]}{\sigma_f \sigma_{\text{class}}} \quad (2)$$

253 The *corrFeatureEval* is also a fast filter-based feature selection technique.
 254 The features selected (based on the threshold) are ranked in the decreasing
 255 order of PCC scores.

256 *3.2.3. Correlation-based feature subset selection*

257 Correlation-based feature subset selection (*cfsSubsetEval*) [24] considers the
 258 redundancy between the features and the individual predictive ability of fea-
 259 tures, to evaluate the goodness (worth) of a feature subset. Subsets with lower
 260 inter-correlation and high correlation with the target class are chosen. The
 261 worth of a feature subset S with k features is given by Equation 3, where \mathcal{C}
 262 measures the relatedness of two variables (correlation, not necessarily Pearson’s
 263 correlation or Spearman’s ρ).

$$\text{Worth}(S_k) = \frac{\sum_{f_i \in S_k} \mathcal{C}(f_i, \text{class})}{\sqrt{\sum_{f_i \in S_k} \sum_{f_j \in S_k - \{f_i\}} \mathcal{C}(f_i, f_j)}} \quad (3)$$

264 Symmetric uncertainty [65], an entropy-based measure of relatedness is used
 265 in this paper. Symmetric uncertainty between two variables X_i, X_j is given by

266 Equation 4, where $\text{MI}(X_i, X_j)$ measures the mutual information between X_i ,
 267 X_j and $H(\cdot)$ represents the marginal entropy.

$$\text{Uncertainty}(X_i, X_j) = 2 \cdot \frac{\text{MI}(X_i, X_j)}{H(X_i) + H(X_j)} \quad (4)$$

268 The subspace of feature subsets is searched forward, starting with an empty
 269 feature subspace, by greedy hillclimbing with backtracking. Note that this
 270 search approach provides no feature ranking.

271 3.2.4. Minimum redundancy maximum relevance

272 Minimum Redundancy Maximum Relevance (*mRMR*) [52] is an incremen-
 273 tal search method which integrates relevance and redundancy into a single
 274 objective function that aims at maximizing relevance and minimizing redun-
 275 dancy. The scoring function can combine redundancy and relevance as: 1)
 276 relevance–redundancy, which is Mutual Information Difference (MID) or 2)
 277 relevance/redundancy, which is Mutual Information Quotient (MIQ). The MID
 278 objective function (Φ) used to achieve *mRMR* is given by Equation 5, where
 279 $\text{MI}(X_i, X_j)$ measures the mutual information between X_i, X_j .

$$\Phi = \frac{1}{|S_k|} \sum_{f_i \in S_k} \text{MI}(f_i, \text{class}) - \frac{1}{|S_k|^2} \sum_{f_i, f_j \in S_k} \text{MI}(f_i, f_j) \quad (5)$$

280 The *mRMR* approach is used with C4.5 decision trees (information gain).
 281 This feature selection approach ranks in decreasing order, the selected features
 282 (based on the threshold) based on *mRMR* scores.

283 3.2.5. OneR-based feature selection

284 OneR-based feature selection (*oneRFeatureEval*) [48] evaluates the worth of
 285 a feature by using OneR as the filter to select features, by recursive elimination.
 286 The OneR algorithm aims at deducing a rule that predicts the target class based
 287 on the given values of the features. The algorithm chooses the feature with more
 288 information and forms an entire rule based on that feature [7].

289 The *oneRFeatureEval* technique uses a rule to evaluate the usefulness of
 290 features. The selected features (based on the threshold) are ranked in the order
 291 of decreasing OneR rule scores.

292 3.3. Classification algorithms

293 Three classification algorithms from the existing literature including Random
 294 Forest (RF) [26], Bootstrap Aggregating with C4.5 Decision Trees (BDT) [11],
 295 and K-Nearest Neighbors (KNN) [53] are used in the evaluation of the predictive
 296 capabilities (in the form of accuracy scores) of the selected informative features.
 297 The implementations available in the Python Scikit-learn package were used to
 298 implement all the classifiers used in this paper.

299 Random Forest [26] is an ensemble learning technique that operates by con-
 300 structing a number of decision trees while training. RF predicts the target class
 301 as the mode of the classes of individual trees. Bootstrap Aggregating (Bagging)

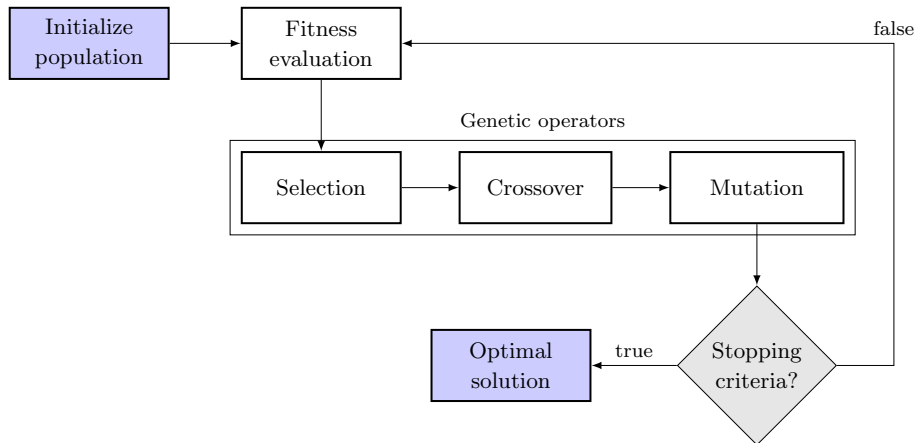


Figure 1: The flow of the genetic algorithm used in the optimization of the penalty parameters.

302 [11] is a machine learning ensemble meta-algorithm that improves the stability
 303 and accuracy of machine learning algorithms (here, decision trees). Bagging is
 304 a special case of the averaging technique. The method reduces variance and
 305 avoids overfitting. K-Nearest Neighbors [53] is an instance-based (lazy) learner
 306 that uses the majority vote of its k closest neighbors (distance between the data
 307 points gives a measure of their closeness) to determine the target class.

308 In this paper, RF classifier was used with 100 classification and regression
 309 trees of maximum depth 2. Furthermore, BDT classifier was used with an en-
 310 semble of 100 C4.5 decision trees as base estimators to obtain diversity among
 311 the base trees. Finally, 15 closest neighbors were considered (empirically deter-
 312 mined using grid search) in this analysis, where closeness was weighted as the
 313 inverse of the distance between instances.

314 3.4. Genetic algorithm

315 The Genetic Algorithm (GA) [46] is a bio-inspired metaheuristic belonging
 316 to the class of evolutionary algorithms. Evolutionary algorithms are essentially
 317 swarm intelligence based heuristic search methods. The GA was implemented
 318 in Python 2.7.

319 In solving optimization problems, the idea of GA is that they start with
 320 a randomly generated population of individual solutions. The fitness function
 321 measures the quality of an individual in the population. Genetic operators aid
 322 in the conversion of one generation into the next one. The first operator is the
 323 selection operation which aims at selecting a portion of the existing population
 324 that breeds into the next generation. Individuals are selected based on their
 325 fitness scores, and higher fitness scores imply higher reproductive capability.
 326 Thus the fittest individuals are more likely to be selected while individuals with
 327 lower fitness scores may not be selected for reproduction [66]. The next step
 328 is to generate a new population using crossover (recombination) and mutation.

Table 4: Summary of the stratified samples used in hybrid feature selection.

Sample	Feature space	Summary
\mathcal{S}_1	#Features(dataset)	Feature selection using the chosen methods
\mathcal{S}_2	#Features(\mathcal{S}_1)	Evaluation of the selected features and deriving the hybrid feature subspace
\mathcal{S}_3	Hybrid	Evaluation of the hybrid feature subspace

329 Crossover and mutation aim at replicating the randomness in any evolutionary
 330 process. For every new population produced, a pair of parent individuals are
 331 chosen for breeding and thus the child produced as a result of crossover and
 332 mutation shares many characteristics of the parents. The overall flow of GA is
 333 shown in Figure 1.

334 The genetic operators ensure that the subsequent generation population of
 335 chromosomes is different from the previous one. More often than not, the average
 336 fitness of the new generation will have increased, as only the best individuals
 337 from the previous generation are chosen for breeding, together with a small pro-
 338 portion of less fit individuals which ensures the genetic diversity within the pool
 339 of parents and thus ensures the genetic diversity within the children of the next
 340 generation.

341 In this paper, GA is used to determine the optimal values of the penalty factors
 342 that determine how different feature subspaces can be effectively combined.
 343 Thus the size of each chromosome is equal to the number of penalty parameters,
 344 and the population size is set to 50 to achieve optimal intensification and
 345 diversification within the given number of iterations. Furthermore, GA is im-
 346 plemented with roulette-wheel selection (fitness-proportionate selection) [21], a
 347 crossover factor (P_c) of 0.6, and a mutation factor (P_m) of 0.1 (for a maximum
 348 of 25 iterations).

349 **4. Proposed novel filter-wrapper hybrid greedy ensemble approach** 350 **for optimal feature selection**

351 The proposed filter-wrapper hybrid feature selection approach uses three
 352 samples that are derived from the dataset using stratified random sampling
 353 [49]. Division of population into strata reduces the computational complexity
 354 and the sampling error. The first sample (\mathcal{S}_1) is used in selecting features from
 355 the predetermined feature selection technique(s) (five here). The feature space
 356 of the second sample (\mathcal{S}_2) is then reduced to the set of features selected using
 357 \mathcal{S}_1 . Then, \mathcal{S}_2 is evaluated using the selected classifier(s) (three here). Based on
 358 the features selected in \mathcal{S}_1 and the accuracies obtained from the evaluation of
 359 \mathcal{S}_2 , the feature subspace for the third sample (\mathcal{S}_3) is determined greedily using
 360 penalty parameters. Table 4 summarizes the use of stratified samples in hybrid
 361 feature selection. Figure 2 presents an overview of the proposed hybrid greedy
 362 ensemble approach and additional details of the same are presented below.

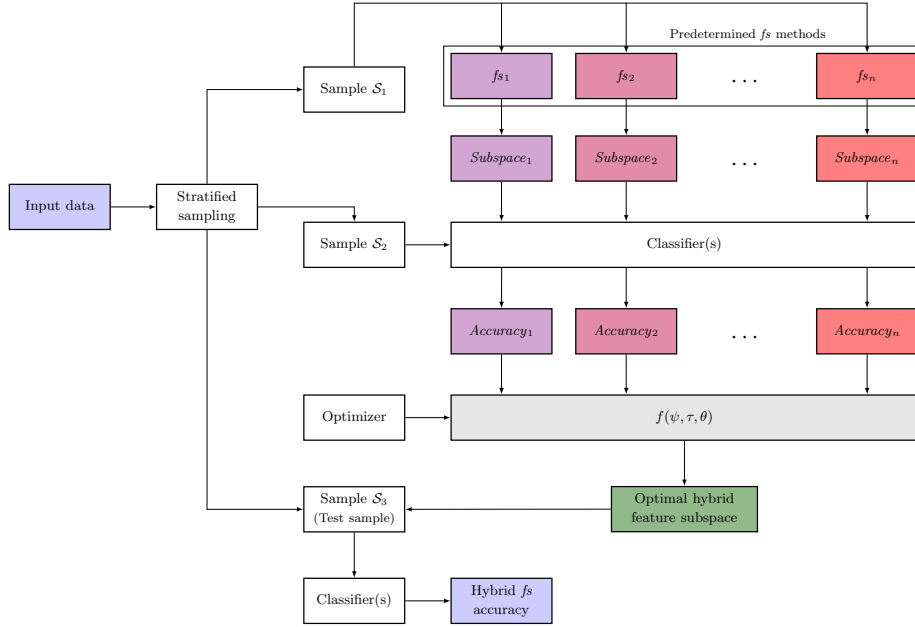


Figure 2: An overview of the proposed greedy hybrid ensemble feature selection modeled from a set of n (five here) predetermined feature selection methods (fs_i s).

363 *4.1. Scoring of features and feature selection methods*

364 The feature subspaces obtained (one for every feature selection technique,
 365 five here) from \mathcal{S}_1 are used to derive the feature scores (*featScore*). The feature
 366 score of a feature f with respect to a feature selection method (with the feature
 367 subspace \mathcal{FS} of length $|\mathcal{FS}|$) with rank $\rho_f (= index(f) + 1)$ ³ is derived using
 368 the Equation 6.

$$featScore(f, \mathcal{FS}, \rho_f) = \begin{cases} \frac{|\mathcal{FS}| - \rho_f + 1}{|\mathcal{FS}|}, & f \in \text{ranked } \mathcal{FS} \\ \frac{1}{|\mathcal{FS}|}, & f \in \text{unranked } \mathcal{FS} \\ \frac{-1}{|\mathcal{FS}|}, & f \notin \mathcal{FS} \end{cases} \quad (6)$$

369 Feature scores can be positive or negative depending on the presence or ab-
 370 sence of a feature in the given feature subspace. Also, it can be noted that
 371 *featScore* gives importance to selecting a lesser number of features, thus achiev-
 372 ing the very aim of dimensionality reduction.

373 The accuracy scores obtained (one for every feature selection method, five
 374 here⁴) from \mathcal{S}_2 are used to derive the scores of the chosen base feature selection
 375 techniques (*accScore*). The *accScore* of a feature selection method m from the

³The rank ρ_f is only calculated when features in \mathcal{FS} are ranked.

⁴The average accuracy of RF, BDT, and KNN is considered for simplicity.

376 set of chosen base feature selection methods \mathcal{M} ($|\mathcal{M}| = 5$ here) with rank ρ_m ($=$
 377 $index(m) + 1$, $m \in \mathcal{M}$ ranked in the decreasing order of accuracies) is derived
 378 using the Equation 7.

$$accScore(m, \mathcal{M}, \rho_m) = \frac{|\mathcal{M}| - \rho_m + 1}{|\mathcal{M}|} \quad (7)$$

379 The accuracy scores are positive scores that ensure the selection of many fea-
 380 tures from those feature selection methods with higher accuracy. Furthermore,
 381 the accuracy scores are only positive to account for the possibility of feature se-
 382 lection from a base method with reduced dimensions and comparable but lower
 383 performance.

384 4.2. Penalty parameters for greedy ensembling of base feature subspaces

385 Penalty parameters facilitate performance dependent greedy selection of op-
 386 timal features from the base selection techniques. They affect the extent of the
 387 impact of both the informativeness of the features and the classification accuracy
 388 of the base selection methods. The accuracy penalty (ψ) and feature penalty
 389 (τ) aim at penalizing the feature scores and accuracy scores respectively. The
 390 accuracy penalty aims at penalizing feature subspaces of the feature selection
 391 methods with \mathcal{S}_2 accuracy less than the \mathcal{S}_2 accuracy with the entire feature
 392 space. Accuracy penalty reduces the impact of the $accScore$. Concisely, the
 393 $accScore$ becomes $accScore/\psi$.

394 Similarly, the feature penalty aims at increasing the negative impact of those
 395 features which are not selected by a feature selection technique, only when the
 396 \mathcal{S}_2 accuracy of the feature selection technique is greater than the \mathcal{S}_2 accuracy
 397 with the entire feature space. Concisely, the $featScore$ becomes $featScore \times \tau$
 398 (only for features with a negative $featScore$).

399 4.3. Overall feature scoring and hybrid feature selection

400 Overall scoring aims at combining the feature scores and accuracy scores to
 401 obtain the overall score which helps in the determination of the greedily selected
 402 most optimal hybrid feature subspace. Overall feature score of a feature f with
 403 respect to the given set of base selection methods \mathcal{M} is given by the Equation
 404 8.

$$overallScore(f, \mathcal{M}) = \sum_m^{\mathcal{M}} featScore(f) \times accScore(m) \quad (8)$$

405 By setting the decision parameter (threshold (θ)), we can filter the features
 406 based on their overall feature scores. The decision parameter aims at selection
 407 higher-ranked ($|\mathcal{FS}| - \rho_f + 1$) features from better performing base selection
 408 methods. The features thus selected form the greedily selected optimal hybrid
 409 feature subspace. Table 5 summarizes the scores and parameters used in the
 410 proposed greedy ensemble hybrid selection approach. Hereafter, the decision
 411 parameter (θ) is referred to as a penalty parameter as it affects the selection

Table 5: Summary of the scores and parameters used in hybrid feature selection.

Parameter	Inference	Summary
$featScore$	Positive or negative scores	Ensures that the hybrid feature subspace is formed from the features selected by the base methods
$accScore$	Positive scores	Ensures the selection of features from high accuracy feature selection methods
ψ	Reduces impact of $accScore$	Penalizes the selection of features from base methods (fs_i) with \mathcal{S}_3 accuracy $< \mathcal{S}_3$ accuracy with entire feature space (fs_{nil})
τ	Increases negative impact of $featScore$	Penalizes the selection of features not selected in a feature selection technique (only when method's \mathcal{S}_3 accuracy $> \mathcal{S}_3$ accuracy with entire feature space (fs_{nil}))
θ	Selection criteria	Determines the number of features to be selected based on the $overallScore$

412 process through overall scores which are penalized by both accuracy and feature
 413 penalties.

414 Algorithm 1 depicts the procedure to obtain the ensembled optimal hy-
 415 brid feature subspace greedily from a given list of feature subsets (\mathcal{FS} -Lists),
 416 \mathcal{S}_2 -Accuracies, \mathcal{S}_2 accuracy with the entire feature space (\mathcal{S}_2 -All-Features-Acc),
 417 total number of features (totalFeat), accuracy rank list (ρ_m -List) and penalty
 418 parameters (ψ , τ , θ). Note that Algorithm 1 assumes that the penalty param-
 419 eters are optimized prior to the greedy feature search.

420 4.4. Optimization of the penalty parameters

421 Optimization of the penalty parameters (ψ , τ , θ) used in the deduction of the
 422 optimal hybrid feature subspace is mandatory as these parameters determine the
 423 greedy selection of features from the base feature subspaces. We leverage heuris-
 424 tic search strategies such as greedy parameter-wise optimization and GA to ob-
 425 tain the best selection results. Compared to the traditional search strategies,
 426 heuristic approaches do not need any domain knowledge and do not make any
 427 assumptions about the search space. Furthermore, heuristic search strategies
 428 can reveal multiple optimal solutions in a single run. In greedy parameter-wise
 429 optimization, the penalty parameters are varied greedily starting with the accu-
 430 racy penalty (ψ), followed by the feature penalty (τ), and finally the threshold
 431 (θ) to obtain the optimal values of these parameters. In GA, the initial gener-
 432 ation of population solutions are generated by selecting random values in the
 433 predetermined range(s) (dataset dependent). The predetermined ranges were
 434 set with higher feature penalty range and comparably lower accuracy penalty
 435 range. Higher feature penalty range was set to heavily penalize those less dis-
 436 criminative features that were not selected by better performing base methods
 437 but were selected by methods with lower performance. Lower accuracy penalty

Algorithm 1: Proposed hybrid greedy ensemble feature selection

Input: $\mathcal{S}_2_All_Features_Acc$: Average accuracy with all features of \mathcal{S}_2 ,
 $\mathcal{S}_2_Accuracies$: List of average accuracies from predetermined methods,
 $\mathcal{FS_Lists}$: List of all selected feature subsets,
 $totalFeat$: Total number of features in the given dataset,
 ρ_m_List : List of ranks of predetermined selection methods,
 ψ : Accuracy penalty parameter,
 τ : Feature penalty parameter,
 θ : Selection threshold.

Output: Hybrid \mathcal{FS} : Greedily selected optimal feature subset.

```
1: accScores  $\leftarrow$  [0] *  $|\mathcal{FS\_Lists}|$ 
2: overallScores  $\leftarrow$  [0] * totalFeat
3: for  $idx \leftarrow 0$  to  $|\mathcal{FS\_Lists}|$  do
4:   accScores[idx]  $\leftarrow$  accScore(method,  $|\mathcal{FS\_Lists}|$ ,  $\rho_m\_List[idx]$ )
5:   if  $\mathcal{S}_2\_Accuracies[idx] < \mathcal{S}_2\_All\_Features\_Acc$  then
6:     accScores[idx]  $\leftarrow$  accScores[idx]/ $\psi$ 
7:   end
8:   for  $featIdx \leftarrow 0$  to totalFeat do
9:     featScore  $\leftarrow$  featScore(feat,  $\mathcal{FS\_Lists}[idx]$ , featIdx + 1)
10:    if  $\mathcal{S}_2\_Accuracies[idx] > \mathcal{S}_2\_All\_Features\_Acc$  and feat  $\notin \mathcal{FS\_Lists}[idx]$  then
11:      featScore  $\leftarrow$  featScore *  $\tau$ 
12:    end
13:    overallScore  $\leftarrow$  featScore * accScores[idx]
14:    overallScores[featIdx]  $\leftarrow$  overallScores[featIdx] + overallScore
15:  end
16: end
17: hybridFeatures  $\leftarrow$  []
18: for  $score \in overallScores$  do
19:   if  $score > \theta$  then
20:     hybridFeatures.append(feat)
21:   end
22: end
23: return hybridFeatures
```

438 range accounts for the possibility of selection from a base method with reduced
439 dimensions and comparable but lower performance. Furthermore, the minimum
440 number of features to be selected was set to $0.1 \times$ the total number of features to
441 reject extremely low dimensional feature subspaces resulting in near-zero per-
442 formance. The fitness function used to evaluate individuals is the average of
443 \mathcal{S}_3 (with features of the hybrid subspace) accuracies obtained using RF, BDT,
444 and KNN classifiers with 10-fold cross-validation. The stopping criteria for GA
445 was achieved when either the optimal solution convergence or a limit on the
446 maximum of iterations was reached. The flow of the proposed hybrid greedy
447 ensemble feature selection optimized using GA is illustrated in Figure 3.

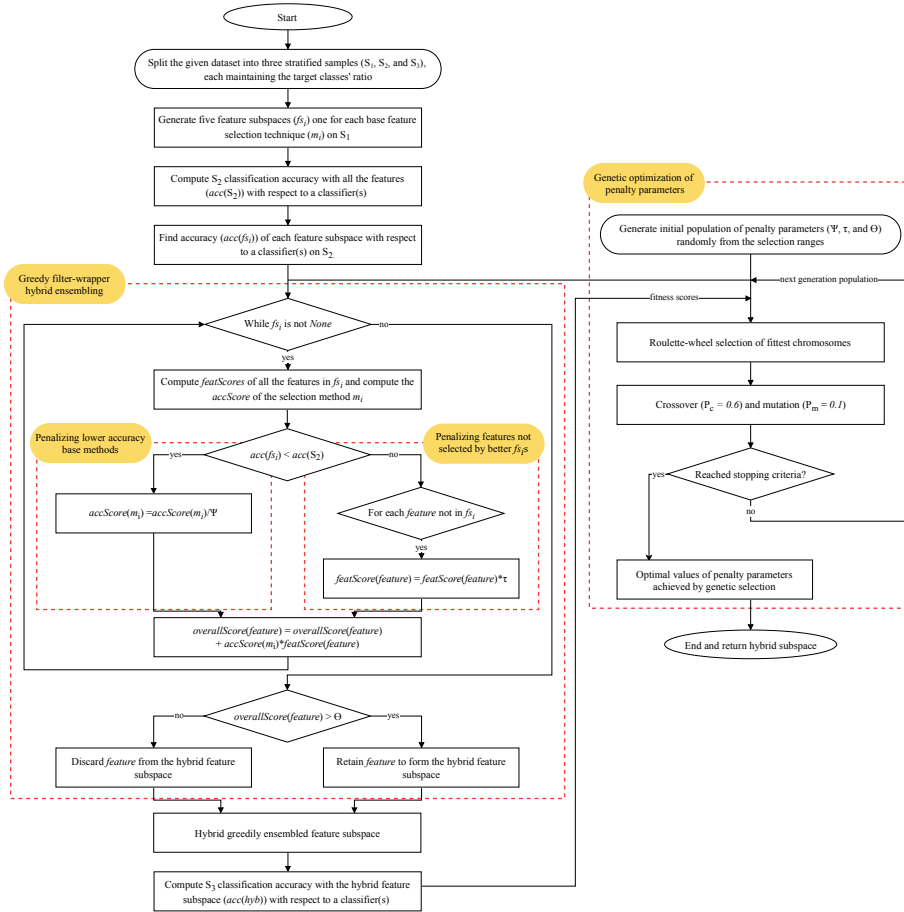


Figure 3: The main process of the proposed hybrid greedy ensemble feature selection optimized using GA.

448 **5. Experimental results and discussion**

449 In this section, we report a detailed benchmarking of our filter-wrapper hybrid
 450 greedy ensemble approach on three high-dimensional biomedical datasets.
 451 We first describe the implementation setup, the working environment, and the
 452 validation procedure used. Then we discuss the parameter setup, their affect
 453 on the proposed system, and the performance of the proposed model, followed
 454 by its complexity analysis and training details. Finally, we elucidate on the
 455 implications of using our proposed hybrid ensemble in real-world biomedical
 456 applications.

457 *5.1. Experimental setup and validation*

458 To investigate the effectiveness of the proposed filter-wrapper hybrid greedy
 459 ensemble feature selection approach, we carried out a detailed benchmarking on

Table 6: Parameters used in the proposed hybrid greedy ensemble approach.

	Greedy parameter-wise optimization	Genetic selection of optimal parameters
ψ	1 – 1.5	1 – 10
τ	1 – 10	1 – 25
θ	0 – 1	Dataset-specific
Scaling factor	ψ : 0.1, τ : 2, and θ : 0.2	–
P_c and P_m	–	0.6 and 0.1

460 three high-dimensional biomedical datasets (see Table 3). Experiments related
 461 to hybrid feature selection were performed on a PC with Intel Core i5 4×1.8
 462 GHz CPU with 8 GB RAM in the MAC 10.14 OS and the experiments related
 463 to parameter optimization were performed on a server with Intel Xeon 2×2.40
 464 GHz processor with 8 GB RAM and 1×TESLA C-2050 (3 GB memory). All
 465 the experiments were coded in Python 2.7 and Weka 3.8.3. All the experiments
 466 were carried out by 10-fold cross-validation, and the overall performance was
 467 estimated as the average across all folds. The biomedical datasets have adequate
 468 samples to aid in the creation of three stratified samples. Furthermore, two
 469 balanced (TIS [51] and Skin Cancer [63]) and one imbalanced (Seizure [5]) high-
 470 dimensional datasets were chosen for an unbiased evaluation of the proposed
 471 technique.

472 Accuracy was used as the standard performance evaluation metric in this
 473 paper. Accuracy computes the average number of correct predictions over the
 474 given samples. Accuracy with $\mathcal{Y}_{\text{true}}$ ground truth labels, $\mathcal{Y}_{\text{pred}}$ predicted class
 475 labels, and $I(x, y)$ indicator function that returns 1 only when $x = y$, can be
 476 defined as in Equation 9.

$$\text{Accuracy}(\mathcal{Y}_{\text{true}}, \mathcal{Y}_{\text{pred}}) = \frac{1}{\#\text{samples}} \sum_{i=1}^{\#\text{samples}} I(\mathcal{Y}_{\text{true}_i}, \mathcal{Y}_{\text{pred}_i}) \quad (9)$$

477 Furthermore, to simplify the evaluation, the accuracy computed for three
 478 classifiers used in this paper (RF, BDT, and KNN) were aggregated by averaging
 479 the individual accuracy scores.

480 5.2. Parameter setup and performance benchmarking

481 The ranges of the penalty parameters must be preset to facilitate the en-
 482 sembling of the base feature selection approaches in the most optimal way. The
 483 predetermined ranges were set with a higher τ range and comparably lower
 484 ψ range. A higher τ range was set to heavily penalize those less informative
 485 features that were not selected by the better performing base feature selection
 486 methods but were selected by methods with lower performance. Lower ψ range
 487 accounts for the possibility of selection from a base method with reduced di-
 488 mensions and comparable but lower performance. While the ranges of τ and ψ

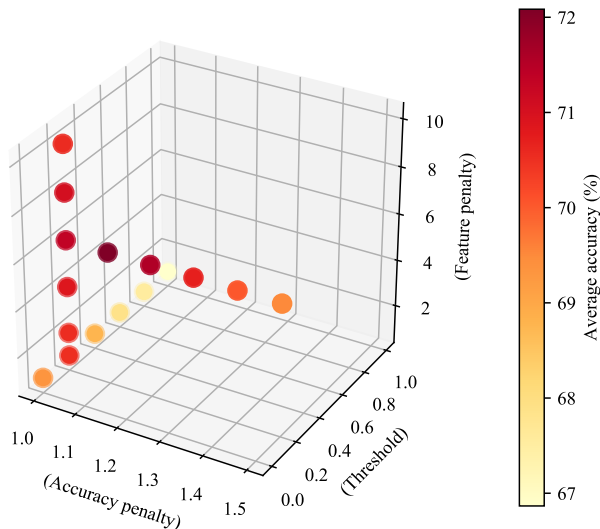


Figure 4: The effect of ψ , τ , and θ on the proposed hybrid feature selection technique using the Skin Cancer dataset [63].

489 can be set greedily by hillclimbing for an optimal range, θ is highly reliant on
 490 the overall scores of the features. The range of θ is set from the minimum of all
 491 *overallScore* values to the maximum of all *overallScore* values. In the case of
 492 greedy parameter-wise optimization, θ was set from 0.0 to 1.0 since this range
 493 was common to all the datasets used in this paper.

494 In the case of greedy parameter-wise optimization, an empirical analysis
 495 was conducted to evaluate the variations in the accuracy with the change in
 496 the penalty parameters (ψ , τ , and θ). Figure 4 shows the variations in the
 497 hybrid feature selection accuracy on the Skin Cancer dataset [63] with respect
 498 to penalty parameters ψ ranging from 1 to 1.5 (increments of 0.1), τ ranging
 499 from 1 to 10 (increments of 2) and θ ranging from 0.0 to 1.0 (increments of 0.2)
 500 as a heat map.

501 Table 7⁵ and Table 8⁵ present detailed insights into the empirical analysis
 502 performed on the Skin Cancer dataset [63] using greedy parameter-wise opti-
 503 mization. In Table 7 and Table 8 the parameters were greedily selected, starting
 504 with θ (varied from 0.0 to 1.0 (increments of 0.2)), followed by τ (varied from 1
 505 to 10 (increments of 2)), and ψ (varied from 1 to 1.5 (increments of 0.1)). The

⁵ fs_{hyb} denotes the proposed hybrid feature selection, fs_{nil} denotes no feature selection, and fs_1 to fs_5 denote the base feature selection methods in the order of *cfsSubsetEval*, *mRMR*, *oneRFeatureEval*, *corrFeatureEval*, and *igFeatureEval*.

Table 7: The effect of ψ , τ , and θ on the proposed hybrid feature selection technique using the Skin Cancer dataset [63].

ψ	τ	θ	Number of selected features							Classifier	\mathcal{S}_3 accuracy (%)						
			fs_{hyb}	fs_{nil}	fs_1	fs_2	fs_3	fs_4	fs_5		fs_{hyb}	fs_{nil}	fs_1	fs_2	fs_3	fs_4	fs_5
1	1	0	275	2352	66	32	100	121	100	RF	71.5698	70.4014	70.1618	69.5626	70.9100	69.8322	69.0833
										BDT	70.3116	69.7723	68.9934	69.2630	69.2930	68.9934	68.0348
										KNN	66.1474	65.2187	62.4326	62.5225	65.3984	63.0917	62.8820
1	1	0.2	99	2352	66	32	100	121	100	RF	73.2217	70.4014	70.1618	69.5626	70.9100	69.8322	69.0833
										BDT	71.2630	69.7723	68.9934	69.2630	69.2930	68.9934	68.0348
										KNN	67.1216	65.2187	62.4326	62.5225	65.3984	63.0917	62.8820
1	1	0.4	64	2352	66	32	100	121	100	RF	71.2217	70.4014	70.1618	69.5626	70.9100	69.8322	69.0833
										BDT	69.5630	69.7723	68.9934	69.2630	69.2930	68.9934	68.0348
										KNN	65.5216	65.2187	62.4326	62.5225	65.3984	63.0917	62.8820
1	1	0.6	50	2352	66	32	100	121	100	RF	70.2217	70.4014	70.1618	69.5626	70.9100	69.8322	69.0833
										BDT	69.2730	69.7723	68.9934	69.2630	69.2930	68.9934	68.0348
										KNN	64.1216	65.2187	62.4326	62.5225	65.3984	63.0917	62.8820
1	1	0.8	34	2352	66	32	100	121	100	RF	69.9290	70.4014	70.1618	69.5626	70.9100	69.8322	69.0833
										BDT	68.8472	69.7723	68.9934	69.2630	69.2930	68.9934	68.0348
										KNN	63.8890	65.2187	62.4326	62.5225	65.3984	63.0917	62.8820
1	1	1	21	2352	66	32	100	121	100	RF	69.3829	70.4014	70.1618	69.5626	70.9100	69.8322	69.0833
										BDT	68.5740	69.7723	68.9934	69.2630	69.2930	68.9934	68.0348
										KNN	62.6423	65.2187	62.4326	62.5225	65.3984	63.0917	62.8820
1	2	0.2	98	2352	66	32	100	121	100	RF	73.2441	70.4014	70.1618	69.5626	70.9100	69.8322	69.0833
										BDT	71.2700	69.7723	68.9934	69.2630	69.2930	68.9934	68.0348
										KNN	67.1311	65.2187	62.4326	62.5225	65.3984	63.0917	62.8820
1	4	0.2	90	2352	66	32	100	121	100	RF	73.6821	70.4014	70.1618	69.5626	70.9100	69.8322	69.0833
										BDT	71.4173	69.7723	68.9934	69.2630	69.2930	68.9934	68.0348
										KNN	67.5230	65.2187	62.4326	62.5225	65.3984	63.0917	62.8820

Table 8: The effect of ψ , τ , and θ on the proposed hybrid feature selection technique using the Skin Cancer dataset [63] (contd.).

ψ	τ	θ	Number of selected features							Classifier	\mathcal{S}_3 accuracy (%)						
			fs_{hyb}	fs_{nil}	fs_1	fs_2	fs_3	fs_4	fs_5		fs_{hyb}	fs_{nil}	fs_1	fs_2	fs_3	fs_4	fs_5
1	6	0.2	80	2352	66	32	100	121	100	RF	74.1121	70.4014	70.1618	69.5626	70.9100	69.8322	69.0833
										BDT	72.0360	69.7723	68.9934	69.2630	69.2930	68.9934	68.0348
										KNN	67.9131	65.2187	62.4326	62.5225	65.3984	63.0917	62.8820
1	8	0.2	72	2352	66	32	100	121	100	RF	74.0230	70.4014	70.1618	69.5626	70.9100	69.8322	69.0833
										BDT	71.8850	69.7723	68.9934	69.2630	69.2930	68.9934	68.0348
										KNN	67.2371	65.2187	62.4326	62.5225	65.3984	63.0917	62.8820
1	10	0.2	70	2352	66	32	100	121	100	RF	73.5461	70.4014	70.1618	69.5626	70.9100	69.8322	69.0833
										BDT	71.4010	69.7723	68.9934	69.2630	69.2930	68.9934	68.0348
										KNN	66.7712	65.2187	62.4326	62.5225	65.3984	63.0917	62.8820
1.1	6	0.2	73	2352	66	32	100	121	100	RF	74.6113	70.4014	70.1618	69.5626	70.9100	69.8322	69.0833
										BDT	72.3316	69.7723	68.9934	69.2630	69.2930	68.9934	68.0348
										KNN	69.3110	65.2187	62.4326	62.5225	65.3984	63.0917	62.8820
1.2	6	0.2	70	2352	66	32	100	121	100	RF	74.0120	70.4014	70.1618	69.5626	70.9100	69.8322	69.0833
										BDT	71.9162	69.7723	68.9934	69.2630	69.2930	68.9934	68.0348
										KNN	68.7710	65.2187	62.4326	62.5225	65.3984	63.0917	62.8820
1.3	6	0.2	68	2352	66	32	100	121	100	RF	73.1211	70.4014	70.1618	69.5626	70.9100	69.8322	69.0833
										BDT	70.9913	69.7723	68.9934	69.2630	69.2930	68.9934	68.0348
										KNN	68.0110	65.2187	62.4326	62.5225	65.3984	63.0917	62.8820
1.4	6	0.2	64	2352	66	32	100	121	100	RF	72.5810	70.4014	70.1618	69.5626	70.9100	69.8322	69.0833
										BDT	69.7113	69.7723	68.9934	69.2630	69.2930	68.9934	68.0348
										KNN	67.8103	65.2187	62.4326	62.5225	65.3984	63.0917	62.8820
1.5	6	0.2	62	2352	66	32	100	121	100	RF	72.0180	70.4014	70.1618	69.5626	70.9100	69.8322	69.0833
										BDT	69.4391	69.7723	68.9934	69.2630	69.2930	68.9934	68.0348
										KNN	67.0410	65.2187	62.4326	62.5225	65.3984	63.0917	62.8820

Table 9: Comparison of the average accuracies of the proposed hybrid feature selection technique optimized using GA (top ten chromosomes) over the base methods.

Dataset	Chromosome			\mathcal{S}_3 average accuracy (%)	
	ψ	τ	θ	$f_{s_{\text{hyb}}}$	Base selection methods
TIS [51]	6.08	20.63	0.78	87.449	
	9.04	18.46	1.54	86.795	
	9.04	18.46	1.57	86.264	$f_{s_{\text{nil}}}$: 81.787
	9.04	9.34	1.29	86.137	f_{s_1} : 83.506
	1.05	24.06	0.58	85.592	f_{s_2} : 73.391
	1.05	18.46	0.99	85.562	f_{s_3} : 80.153
	8.12	24.06	0.58	85.434	f_{s_4} : 83.395
	9.04	18.46	0.65	85.405	f_{s_5} : 83.948
	9.04	9.34	0.80	85.337	
	9.04	24.06	0.25	85.068	
Skin Cancer [63]	1.07	7.72	0.14	78.912	
	1.65	6.77	0.04	78.783	
	1.56	6.17	0.09	78.374	$f_{s_{\text{nil}}}$: 68.464
	1.11	6.07	0.14	78.343	f_{s_1} : 68.534
	1.28	6.77	0.04	78.323	f_{s_2} : 67.306
	1.55	6.46	0.12	78.292	f_{s_3} : 66.667
	1.24	6.67	0.03	78.253	f_{s_4} : 67.116
	2.28	5.97	0.17	68.910	f_{s_5} : 67.196
	1.07	11.87	0.24	67.860	
	1.07	20.72	0.24	67.312	
Seizure [5]	1.39	2.58	0.01	51.811	
	1.31	3.09	0.43	50.822	
	1.62	5.96	0.19	49.422	$f_{s_{\text{nil}}}$: 47.131
	1.16	2.30	0.33	48.517	f_{s_1} : 45.412
	1.92	7.58	-0.05	47.663	f_{s_2} : 46.723
	1.81	1.21	0.11	47.063	f_{s_3} : 45.988
	1.38	8.78	0.20	46.818	f_{s_4} : 44.988
	1.14	9.53	0.31	46.421	f_{s_5} : 45.858
	1.40	9.05	0.41	46.322	
	1.45	9.91	0.41	46.158	

506 threshold was varied initially, to find the best possible value which was then
507 set throughout the analysis. A maximum average accuracy of 70.535% was
508 obtained using $\psi = 1$, $\tau = 1$, and $\theta = 0.2$ (fix θ). Then, the feature penalty
509 was varied to find the best possible value, which was then set. A maximum
510 average accuracy of 71.354% was obtained using $\psi = 1$, $\tau = 6$, and $\theta = 0.2$.

⁶Average of the runtime obtained using RF, BDT, and KNN classifiers.

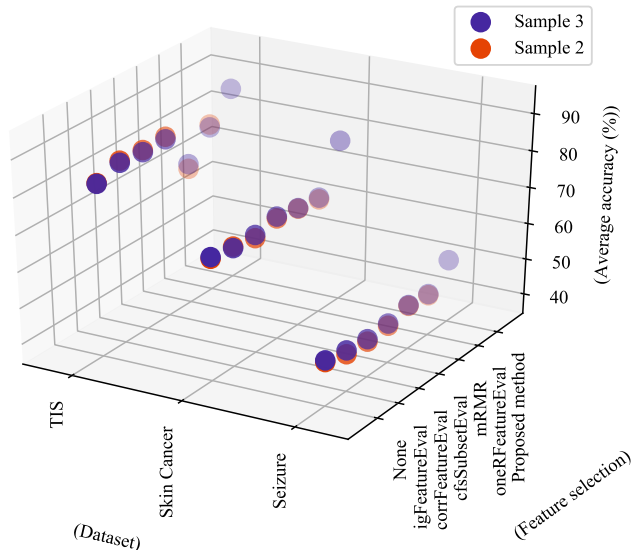


Figure 5: Comparison of the average accuracies of various feature selection methods across different datasets.

511 Finally, the accuracy penalty was varied to find the best possible value. Thus, by
 512 changing the values of the penalty parameters within the preset range, 72.085%
 513 average accuracy (3.6% more than that for any predetermined feature selection
 514 method) was obtained with the penalty parameters $\psi = 1.1$, $\tau = 6$, and $\theta = 0.2$
 515 selected using greedy parameter-wise optimization. Also, it was observed that
 516 our proposed method took an average running time⁶ of 1.283 seconds while
 517 classification using all the features took 18.71 seconds.

518 Figure 5 shows the superiority of the proposed hybrid greedy ensemble
 519 method optimized using GA, in terms of average accuracy over the base fea-
 520 ture selection methods, via empirical analysis. Also, it is interesting to note
 521 from Figure 5 that the samples (\mathcal{S}_2 , \mathcal{S}_3) obtained from stratified sampling were
 522 very similar. Table 9⁵ compares the accuracies obtained using various penalty
 523 parameters optimized by GA with the selected base selection techniques. The
 524 penalty parameters (chromosomes in GA) were varied in the range of 1 to 10 for
 525 ψ , 1 to 25 for τ , and minimum *overallScore* to maximum *overallScore* for θ . The
 526 minimum number of features to be selected was set to $0.1 \times$ the total number
 527 of features, i.e., the penalty parameters resulting in a hybrid feature subspace
 528 with less than the set minimum threshold of features were rejected. Note that
 529 all the top ten chromosomes for the TIS dataset [51], top eight (of ten) chromo-
 530 somes for the Skin Cancer dataset [63], and top five (of ten) chromosomes for
 531 the Seizure dataset [5] outperform the base selection methods. It can be noted

532 that using GA to optimize the penalty parameters produces higher accuracies in
533 comparison to the results obtained using greedy parameter-wise optimization.
534 This can be attributed to the fact that the swarm-intelligence based heuristic
535 search is flexible and versatile, in the sense that they mimic the best features
536 in the nature. It can be observed that the value of ψ must be kept relatively
537 low while the value of τ must be moderately adjusted to obtain an optimal
538 feature subset. This can be attributed to the fact that ψ aims at penalizing
539 those base selection methods with lower \mathcal{S}_2 accuracy than that obtained using
540 the entire feature space, while τ penalizes the features not selected by the better
541 performing feature selection methods (\mathcal{S}_2 accuracy greater than that obtained
542 using entire feature space). Higher accuracy penalty indicates rejection of the
543 features from those base selection techniques with lower accuracy than that ob-
544 tained with no feature selection, implying that that technique was of no use at
545 all in reducing the feature space. It was observed that the optimization of the
546 proposed ensemble using GA took 1.86 hours for TIS dataset [51], 2.31 hours
547 for the Skin Cancer dataset [63], and 1.44 hours for the Seizure dataset [5].

548 From Table 9 it can be noted that the proposed method, when optimized
549 using GA outperforms the base methods by a maximum of 4.17% (3.5% higher)
550 and at least by 1.34% (1.12% higher) for the TIS dataset [51], by a maximum
551 of 15.14% (10.37% higher) and at least by 0.55% (0.38% higher) for the Skin
552 Cancer dataset [63] and by a maximum of 9.93% (4.68% higher) and at least
553 by 1.13% (0.53% higher) for the Seizure Dataset [5]. From the obtained results,
554 the following two major trends were predominantly observed:

- 555 • The genetic selection performs an exhaustive heuristic search leading to
556 better optimization of the values of the penalty parameters as compared to
557 the values obtained using greedy parameter-wise optimization.
- 558 • A significantly lower value of the accuracy penalty (ψ) and a higher value
559 of the feature penalty (τ) often leads to the optimal ensembling of base
560 subspaces to produce the most informative feature subspace.

561 The obtained results indicate the superiority and efficiency and robustness of
562 our proposed hybrid greedy ensemble optimized using GA over the base selection
563 techniques. Furthermore, the proposed greedy ensemble approach was compared
564 with state-of-the-art prolific wrapper methods [57] including Recursive Feature
565 Elimination (RFE) using SVM with linear kernel and RFE using SVM with
566 Radial Basis Function (RBF) kernel [40]. We also compare our results with
567 widely used filter selection approaches including feature importance using RF
568 [70] and chi-square test [47]. Table 10 presents the superiority of the proposed
569 ensemble optimized using GA over prolific filter and wrapper methods. RFE
570 using SVM with linear kernel, feature importance using RF, and chi-square
571 selection approaches were performed on sample \mathcal{S}_2 to retain 100 best features,
572 while RFE using SVM with RBF kernel was programmed to retain about top
573 10% of the features using sample \mathcal{S}_2 . It can be observed that the proposed
574 method outperforms prolific filter methods by 4% for the TIS dataset, 16.4%
575 for the Skin Cancer dataset, and 11.2% for the Seizure dataset. Additionally,

Table 10: Comparison of the proposed hybrid greedy ensemble approach over state-of-the-art prolific filter and wrapper selection approaches.

Dataset	\mathcal{S}_3 average accuracy (%)				Proposed greedy ensemble (GA)
	Filter approaches		Wrapper approaches		
	Feature importance (RF)	Chi-square test	RFE using SVM with linear kernel	RFE using SVM with RBF kernel	
TIS [51]	84.182	84.220	79.968	83.290	87.449
Skin Cancer [63]	67.356	67.794	67.307	67.375	78.912
Seizure [5]	46.601	46.299	46.818	50.450	51.811

576 it can be remarked that the proposed method also outperforms state-of-the-
577 art wrapper methods by 5% for the TIS dataset, 17.12% for the Skin Cancer
578 dataset, and 2.7% for the Seizure dataset.

579 5.3. Computational complexity analysis

580 Concerning the training of the proposed ensemble approach, the feature sub-
581 spaces from various predetermined base selection methods must be computed
582 apriori. Additionally, the genetic selection of the optimal penalty parameters
583 must also be achieved apriori. With the prescient knowledge of the optimal
584 penalty parameters and feature subspaces, the proposed hybrid approach en-
585 sembles the subspaces greedily based on the penalty factors. Thus, the com-
586 putational complexity of the proposed algorithm is heavily reliant on the com-
587 plexity of obtaining predetermined feature subspaces ($= O(fs)$) and the genetic
588 selection of the penalty parameters. It is interesting to note that the computa-
589 tional complexity of the proposed method is significantly reduced by using filter
590 selection methods as the base selection approaches. Furthermore, since the se-
591 lection of features is performed on a sample of the high-dimensional dataset as
592 opposed to the entire dataset, the computational cost is reduced further.

593 To solve real-life optimization problems with less computational volume, an
594 optimization or heuristic search strategy needs to be computationally feasible.
595 To analyze the computational cost of the optimization strategy used in terms
596 of worst-case computation time, the step-wise complexity analysis is performed.
597 The initialization of a population of size P in GA is $O(n \cdot P) \approx O(P)$ complex,
598 where n (constant, 3 here) is the size of each chromosome. The fitness evaluation
599 used in this study is the average of the accuracies obtained from RF, BDT,
600 and KNN classifiers. Assume that computing the average accuracy using these
601 classifiers takes $O(\text{fitness})$ time which is radically dataset dependent. Roulette-
602 wheel measures the area covered by a chromosome in a given population P
603 using the fitness scores. Every chromosome forms a part of the wheel with
604 its slice size proportionate to its fitness score. Roulette-wheel selection can be
605 achieved in $O(P^2)$. Finally, crossover and mutation genetic operations take
606 $O(P_c \cdot O(\text{crossover}))$ and $O(P_m \cdot O(\text{mutation}))$ times respectively. The GA
607 optimization to find optimal penalty parameters is run for G iterations. Since
608 P , G , P_c , and P_m are constant, the worst-case time complexity to optimize

609 penalty parameters simplifies to $O(O(\text{fitness}) \cdot (O(\text{crossover}) + O(\text{mutation})))$
610 ($= O(\text{GA})$). As a result, the worst-case time complexity of the proposed greedy
611 ensemble using GA is $O(O(fs) + O(\text{fitness}) + O(\text{GA}))$. Note that $O(fs)$ is on
612 the sample \mathcal{S}_1 , $O(\text{fitness})$ is on the sample \mathcal{S}_2 , and $O(\text{GA})$ is on the sample \mathcal{S}_3 .

613 5.4. Effectiveness of the proposed greedy ensemble in real-world biomedical ap- 614 plications

615 The richness and variety of datasets available in the biomedical field have
616 opened new horizons for researchers and investigators. The generated biomed-
617 ical big data inherits the curse of dimensionality as one of its characteristics. Ef-
618 fective dimensionality reduction techniques emulate predictive capability while
619 eliminating the noise and curtailing the computational complexity. Time and
620 cost-effective approaches to select the most discriminative and informative fea-
621 tures are indispensable, especially in the fields of bioinformatics and healthcare.
622 The applicability of a feature selection technique to given data is heavily reliant
623 on its ability to match the structure of the problem and maintain only those
624 features that reveal the inherent patterns in the data. Thus there is a need to
625 develop efficient techniques that aid in the optimal ensembling of such selection
626 techniques for better performance aiding the decision-making process.

627 The proposed greedy approach can be used to ensemble a variety of effec-
628 tive selection approaches to generate an optimal feature subspace that cap-
629 tures the inherent nature of the data. The weighted occurrence scheme and the
630 penalty scheme used in the proposed approach aid in the appropriate selection of
631 most informative features. Such an appropriate selection of features needed for
632 clustering, classification, pattern extraction, and prediction of high-dimensional
633 biomedical datasets with hundreds of attributes can be facilitated effectively
634 using the proposed greedy ensembling approach. Furthermore, the proposed
635 approach can prominently aid in the achievement of efficient analysis in various
636 biomedical applications including the analysis of large volumes of genomic data
637 produced daily due to the advancements in the sequencing technology. This is
638 particularly vital as the selection of important genes is essential to discover the
639 knowledge hidden within the genetic code and to identify significant biomarkers.
640 The robustness and flexibility of the proposed approach facilitate the effective
641 feature selection needed for a wide variety of healthcare applications including
642 disease prediction, risk management, and others. The flexibility or the ability
643 to work with any predetermined set of selection methods allows the proposed
644 greedy approach to work effectively to match the problem structure aiding in
645 effective feature selection.

646 6. Sensitivity analysis

647 The experimental results highlight the effectiveness and robustness of the
648 proposed approach over the base selection methods. To further analyze the ob-
649 tained results, a sensitivity analysis was performed. Sensitivity analysis helps
650 in making decisions concerning more than a solution to the given problem [44].

Table 11: Descriptive statistics of the proposed hybrid greedy ensemble approach across various datasets.

Dataset	Minimum value	Maximum value	Mean	Standard deviation
TIS [51]	85.068	87.449	85.904	0.751
Skin Cancer [63]	67.312	78.912	75.336	5.063
Seizure [5]	46.158	51.811	48.102	1.993

Table 12: A paired samples Wilcoxon signed-rank test (two-tailed, $p < 0.05$) for the proposed greedy ensemble against base selection methods across different datasets.

Dataset	Selection method	p -value	z -value	Null hypothesis decision	Significant difference
TIS [51]	None	0.00512	-2.8031	Reject	Yes
	<i>igFeatureEval</i>	0.00512	-2.8031	Reject	Yes
	<i>corrFeatureEval</i>	0.00512	-2.8031	Reject	Yes
	<i>cfsSubsetEval</i>	0.00512	-2.8031	Reject	Yes
	<i>mRMR</i>	0.00512	-2.8031	Reject	Yes
	<i>oneRFeatureEval</i>	0.00512	-2.8031	Reject	Yes
Skin Cancer [63]	None	0.02202	-2.2934	Reject	Yes
	<i>igFeatureEval</i>	0.02202	-2.2934	Reject	Yes
	<i>corrFeatureEval</i>	0.00512	-2.8031	Reject	Yes
	<i>cfsSubsetEval</i>	0.00512	-2.8031	Reject	Yes
	<i>mRMR</i>	0.00512	-2.8031	Reject	Yes
	<i>oneRFeatureEval</i>	0.00512	-2.8031	Reject	Yes
Seizure [5]	None	0.33204	-0.9683	Retain	No
	<i>igFeatureEval</i>	0.00512	-2.8031	Reject	Yes
	<i>corrFeatureEval</i>	0.09296	-1.6818	Retain	No
	<i>cfsSubsetEval</i>	0.00512	-2.8031	Reject	Yes
	<i>mRMR</i>	0.00512	-2.8031	Reject	Yes
	<i>oneRFeatureEval</i>	0.00512	-2.8031	Reject	Yes

651 Sensitivity analysis measures the extent to which the optimal solution is sensi-
652 tive to the change in the input to one or more parameters. The Kolmogorov-
653 Smirnov test of normality revealed that the obtained results were not normally
654 distributed. Thus, a non-parametric paired samples Wilcoxon signed-rank test
655 at 5% significance level was employed to evaluate the significance of the pro-
656 posed hybrid ensemble over the base selection methods across various datasets.
657 The top ten chromosomes were used in the determination of the significance of
658 the proposed approach over base selection methods as it was assumed that the
659 optimal values would converge to the values of the top ten chromosomes after
660 many finite cycles. Table 11 summarizes the statistical analysis of the proposed
661 approach for top ten chromosomes in terms of accuracy (mean) and robustness
662 (standard deviation).

663 Table 12 shows the results of the paired samples Wilcoxon signed-rank test
664 for the proposed greedy ensemble against conventional base selection methods.
665 The null hypothesis claims no significant difference between the proposed greedy

666 approach and a base selection approach. When the significance is greater than
667 5%, the null hypothesis is retained implying no significant improvement using
668 the proposed hybrid approach. From Table 9 it can be observed that the pro-
669 posed approach is significantly better than the base selection approaches except
670 when the features of the Seizure dataset are all used or when they are selected
671 using *corrFeatureEval*. All in all, the proposed hybrid greedy ensemble approach
672 significantly outperforms the chosen base feature selection approaches.

673 7. Conclusions, limitations, and future directions

674 Feature selection in the field of biomedicine and bioinformatics is indispens-
675 able. In this study, we proposed a penalty based filter-wrapper hybrid greedy
676 ensemble approach to facilitate optimal feature selection. The proposed ap-
677 proach greedily selects the features from the subspaces obtained from the pre-
678 determined base selection methods. Specific performance dependent penalty
679 parameters were used to penalize the base feature subspaces essential to achieve
680 the optimal ensembling of those subspaces. At any point in time, only a strati-
681 fied sample and not the entire dataset is not used for computation; the compu-
682 tational complexity is significantly reduced. Furthermore, we leverage effective
683 heuristic search strategies including the greedy parameter-wise optimization and
684 the GA to obtain optimal values of the penalty parameters. Various applica-
685 tions in the field of bioinformatics and healthcare were detailed. Experimental
686 validation using three high-dimensional biomedical datasets proves the superior-
687 ity (in terms of prediction accuracy), efficiency, and robustness of the proposed
688 ensemble approach. The proposed approach is scalable and flexible as it can
689 accommodate (by ensembling) a variety of feature selection approaches. Empir-
690 ically, we showed that the proposed greedy approach outperformed the chosen
691 base feature selection methods by 4.17% for the TIS dataset, by 15.14% for
692 the Skin Cancer dataset and by 9.93% for the Seizure dataset. The proposed
693 approach also outperformed prolific filter and state-of-the-art wrapper methods
694 by a 5% for the TIS dataset, by 17.12% for the Skin Cancer dataset and by
695 11.2% for the Seizure dataset.

696 Although the proposed approach effectively enhances the feature selection,
697 it has some limitations which call for further research on this topic. First, the
698 proposed method requires the existence of a significant number of records in
699 the dataset for precise sampling. Second, the proposed hybrid greedy ensemble
700 approach introduces additional (penalty) parameters. These vital penalty pa-
701 rameters require prior training to obtain the optimal setting in advance. Thus,
702 parameter self-adaptive greedy ensemble or parameter-free greedy ensemble will
703 be a prominent future research direction. Furthermore, we also aim at investi-
704 gating the computational power of a hybrid of various metaheuristics including
705 cuckoo search, firefly optimization, and GA which establishes an optimal balance
706 between intensification and diversification.

707 **Conflict of interest**

708 The authors confirm that there are no known potential conflicts of interest
709 associated with this publication.

710 **Ethical approval**

711 All the procedures performed by either of the authors in this study do not
712 involve any human participants or animals.

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